

Lecture 9 - Panel Data.pdf

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Lecture 9 -
Panel...

Panel Data

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Panel Data

Introduction

Fixed effects

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Panel Data

Introduction

Fixed effects

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Repeated observations

- Repeated observations
 - Panel data
 - Time-series cross section data
 - Clustered data, etc
- Dynamics effects (dynamic treatment regimes)
- Identification strategies
 - Fixed effects
 - Difference-in-differences

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Group Data

- Panel: observe the same units (individuals, firms, countries, schools, etc.) over several time periods
- Time-series cross section: observe different units across time (e.g., different survey rounds of ENOE)
- Clustered data: Natural grouping in the data (e.g., test score data of students across schools)

Panel Data

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Panel Data

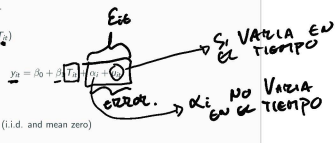
Introduction

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Notation

- Sample of $i = 1, \dots, N$ units from a population
- Time periods $t = 1, \dots, T$
- For each i observe (Y_{it}, X_{it})
- The model is: $Y_{it} = \beta_0 + \beta_1 X_{it} + \alpha_i + u_{it}$
- Do not observe α_i
- Assume u_{it} is white noise (i.i.d. and mean zero)



OLS

- OLS estimator of β_1 on T yields

$$\hat{\beta}_1 = \frac{\text{cov}(T, Y)}{\text{var}(T)}$$

$$= \frac{\text{cov}(T, \beta_0 + \beta_1 T + \alpha_i + u_{it})}{\text{var}(T)}$$

$$= \frac{\text{cov}(T, \beta_0) + \text{cov}(T, \beta_1 T) + \text{cov}(T, \alpha_i) + \text{cov}(T, u_{it})}{\text{var}(T)}$$

$$= \frac{\text{cov}(T, \beta_0)}{\text{var}(T)} + \beta_1 + \frac{\text{cov}(T, \alpha_i)}{\text{var}(T)} + \frac{\text{cov}(T, u_{it})}{\text{var}(T)}$$

Handwritten notes: "Es un error BIEN COMPENSADO" (It is a well-compensated error) and "supuesto cov(T, u_{it}) = 0" (assumption cov(T, u_{it}) = 0).

Simulations!

```

STATA MODEL
beta0 = 0.5
beta1 = 0.2
Nobs = 1000
TimePeriod = 0
* Create individual unobserved factor
Treatment = sample(0, 1)
* Create individual unobserved factor
alpha = rnormal(0, 1)
* Create error term
u = rnormal(0, 1)
* Generate data
forvalues t = 1/1000 {
    replace Y = beta0 + beta1 * X + alpha + u
}
* Estimate OLS
ols OLS, depvar(Y) indepvar(X)
* Show results
coef OLS

```

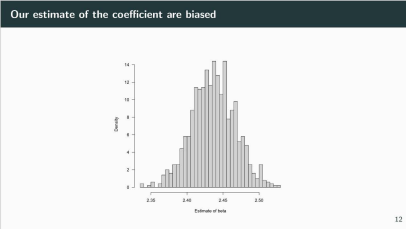
REG
 $Y_{it} = \text{SALARIO}$
 $X_{it} = \text{TITULO UNIV.}$
 $\Rightarrow \text{PARÁMETRO POLÍTICO}$

Simulations!

```

EstimateBeta-MKL
force = 1
alpha = 0.5
beta0 = 0.5
beta1 = 0.2
Nobs = 1000
TimePeriod = 0
* Create individual unobserved factor
Treatment = sample(0, 1)
* Create individual unobserved factor
alpha = rnormal(0, 1)
* Create error term
u = rnormal(0, 1)
* Generate data
forvalues t = 1/1000 {
    replace Y = beta0 + beta1 * X + alpha + u
}
* Estimate OLS
ols OLS, depvar(Y) indepvar(X)
* Show results
coef OLS

```



Fixed effects (intuition I)

- Take one i at a time (like a subset for each i)

$$Y_{i1} = \beta_0 + \beta_1 X_{i1} + \alpha_i + u_{i1}$$

$$\vdots$$

$$Y_{iT} = \beta_0 + \beta_1 X_{iT} + \alpha_i + u_{iT}$$

Handwritten notes: "T OBS DEL INDIVIDUO i" (T observations of individual i) and "SE(B_i) = sigma^2 / sum(X_it^2)" (variance of beta_i estimate).

Simulations!

```

STATA MODEL
beta0 = 0.5
beta1 = 0.2
Nobs = 1000
TimePeriod = 0
* Create individual unobserved factor
Treatment = sample(0, 1)
* Create individual unobserved factor
alpha = rnormal(0, 1)
* Create error term
u = rnormal(0, 1)
* Generate data
forvalues t = 1/1000 {
    replace Y = beta0 + beta1 * X + alpha + u
}
* Estimate OLS
ols OLS, depvar(Y) indepvar(X)
* Show results
coef OLS

```

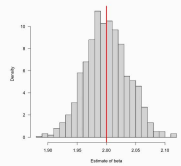
$(\hat{\beta}_i)$ $i=1, \dots, N$
 $\rightarrow SE(\hat{\beta}_i) = \frac{\sigma^2}{\sum(X_{it}^2)}$
 $(X_{it}^2) \approx V(X)$

Simulations!

```

EstimateBeta=MLL
for(i in 1:1000)
  #Data OLS to generate data
  Data=Outcome~beta0+beta1*Data$Treatment+Data$Alpha+resnorm(Nobs*TimePeriods)
  Coefficients=MLL
  VarianceTreatment=MLL
  for(j in 1:Nobs)
    CoefIndividuals=c(Coefficients)
    # Y_ij = beta_0 + beta_1 * Treatment + alpha_i + u_ij
    # alpha_i = ML(Outcome ~ beta0 + beta1 * Treatment | subset(Data$IDObs==j))$coefficients[2]
    Y_ij=Outcome ~ Treatment, data=Data, subset(IDObs==j)$coef[2]
    VarianceTreatment=VarianceTreatment
    var[Data$Treatment[j],Data$IDObs==j]=1
  }
EstimateBeta=(EstimateBeta + weighted.mean(Coefficients, w=VarianceTreatment, na.rm=T))
}
hist(EstimateBeta, freq=F, breaks=30,
     main="hist.coef: Estimates of beta")
abline(v=beta1, col="red", lty=2)
  
```

Our estimate of the coefficient are pretty close to the truth



Fixed effects (intuition II)

- Another idea, is to remove the mean for each observation

$$y_{it} = \beta_0 + \beta_1 T_{it} + \alpha_i + u_{it}$$

$$y_{it} - \bar{y}_i = \beta_1 T_{it} + u_{it} - \bar{u}_i$$

$\bar{y}_i = \beta_0 + \beta_1 \bar{T}_i + \bar{\alpha}_i + \bar{u}_i$ PARA CADA i

$= \alpha_i$

- Estimate via OLS

$Cov(\bar{T}_i, \bar{u}_i) = 0$

Simulations!

```

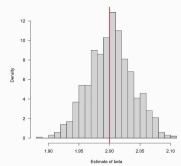
#THE MODEL
beta0=0.5
beta1=0.2
#Generate many observations
Nobs=1000
TimePeriods=10
#Create individual unobserved factor
alpha_i=runif(Nobs)
#Generate many observations
Data=Outcome~beta0+beta1*Data$Treatment+Data$Alpha+resnorm(Nobs*TimePeriods)
#Estimate via OLS
Coefficients=MLL
VarianceTreatment=MLL
for(j in 1:Nobs)
  # Y_ij = beta_0 + beta_1 * Treatment + alpha_i + u_ij
  # alpha_i = ML(Outcome ~ beta0 + beta1 * Treatment | subset(Data$IDObs==j))$coefficients[2]
  Y_ij=Outcome ~ Treatment, data=Data, subset(IDObs==j)$coef[2]
  VarianceTreatment=VarianceTreatment
  var[Data$Treatment[j],Data$IDObs==j]=1
}
EstimateBeta=(EstimateBeta + weighted.mean(Coefficients, w=VarianceTreatment, na.rm=T))
}
hist(EstimateBeta, freq=F, breaks=30,
     main="hist.coef: Estimates of beta")
abline(v=beta1, col="red", lty=2)
  
```

Simulations!

```

EstimateBeta=MLL
for(i in 1:1000)
  Data=Outcome~beta0+beta1*Data$Treatment+Data$Alpha+resnorm(Nobs*TimePeriods)
  Coefficients=MLL
  VarianceTreatment=MLL
  for(j in 1:Nobs)
    CoefIndividuals=c(Coefficients)
    # Y_ij = beta_0 + beta_1 * Treatment + alpha_i + u_ij
    # alpha_i = ML(Outcome ~ beta0 + beta1 * Treatment | subset(Data$IDObs==j))$coefficients[2]
    Y_ij=Outcome ~ Treatment, data=Data, subset(IDObs==j)$coef[2]
    VarianceTreatment=VarianceTreatment
    var[Data$Treatment[j],Data$IDObs==j]=1
  }
EstimateBeta=(EstimateBeta + weighted.mean(Coefficients, w=VarianceTreatment, na.rm=T))
}
hist(EstimateBeta, freq=F, breaks=30,
     main="hist.coef: Estimates of beta")
abline(v=beta1, col="red", lty=2)
  
```

Our estimate of the coefficient are pretty close to the truth



Fixed effects formally

$$y_{it} = \beta_0 + \beta_1 T_{it} + \sum_{j=1}^M 1_{itj} \alpha_j + u_{it}$$

$y_{it} \sim \bar{T}_{it}$

- By the FWL theorem (decomposition theorem) this is equivalent to:
 - OLS of y_{it} with respect to $\sum_{j=1}^M 1_{itj}$, and take the residuals (\tilde{y}_{it})
 - OLS of \bar{T}_{it} with respect to $\sum_{j=1}^M 1_{itj}$, and take the residuals (\tilde{T}_{it})
 - OLS of \tilde{y}_{it} with respect to \tilde{T}_{it}
- OLS with respect to $\sum_{j=1}^M 1_{itj}$ equivalent to subtracting group mean
- Same as the transformation we discussed in the previous slide

$\tilde{y}_{it} = y_{it} - \bar{y}_i$

$\tilde{T}_{it} = T_{it} - \bar{T}_i$

Regressors that are constant within strata

- If a regressor is constant within a fixed-effect strata, then it is perfectly collinear with that strata dummy
- A time-invariant regressor in the panel context
- When you fit fixed effects, these strata-invariant regressors must be dropped
- With fixed effects, what matters is whether the demean variables are constant

Exemple Panel Individual
 Dummy Gender
 Dummy Raza

⇒

Clustering standard errors by fixed effect strata

- We cluster to account for dependencies in the treatment
- If treatments are assigned randomly within fixed effect strata (even if treatment probabilities differ across strata), no need to cluster by strata
- If treatment assignment at the strata level (or treatment exhibits positive or negative dependence within a strata), then cluster by strata
- "felm" from the "lfe" package easiest way in R to do fixed effects and cluster

$$Y_{it} = \alpha_i + \beta' S_{it} + E_{it}$$

↓
 strata

$$E_{it} = \mu_{it} + V_{it}$$

↳

Fixed effects estimators

- Typically we care about β but unit fixed effects α_i could be of interest
- From dummy variable regression is unbiased but not consistent for α_i (based on fixed N and $T \rightarrow \infty$)

Plus ça

$$Y_{it} = \alpha_i + \beta' S_{it} + E_{it}$$

$\alpha_i = \gamma_i$

$$Y_{it} = \beta' S_{it} + E_{it}$$

$$\hat{Y}_{it} = \hat{\alpha}_i + U_{it}$$

$$\sum_{i \in S} \frac{\hat{Y}_{it}}{|S|}$$

es CONSISTENTE
 |S| ES GRANDE
 # ESTUDIANTES

What I will not cover

- Huge literature on panel data
- This is not a review of panel econometrics, for that see Wooldridge and other excellent textbooks
- I won't be covering a lot of it
 - Random effects
 - First difference
 - Arellano and Bond
 - And much more...
- Goal is to present the modal regression model used in difference-in-differences (next class)

FINANZAS
 COO VAO